



Outer Product-based Neural Collaborative Filtering

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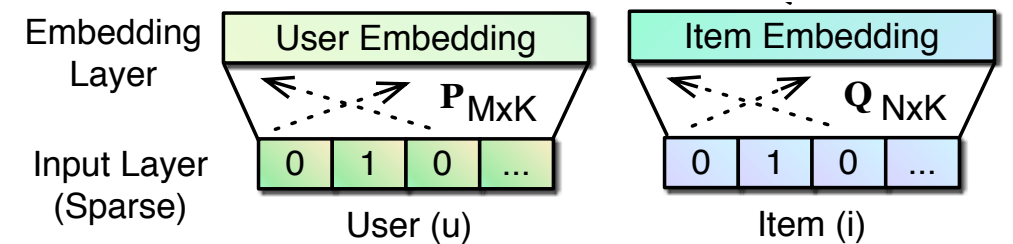
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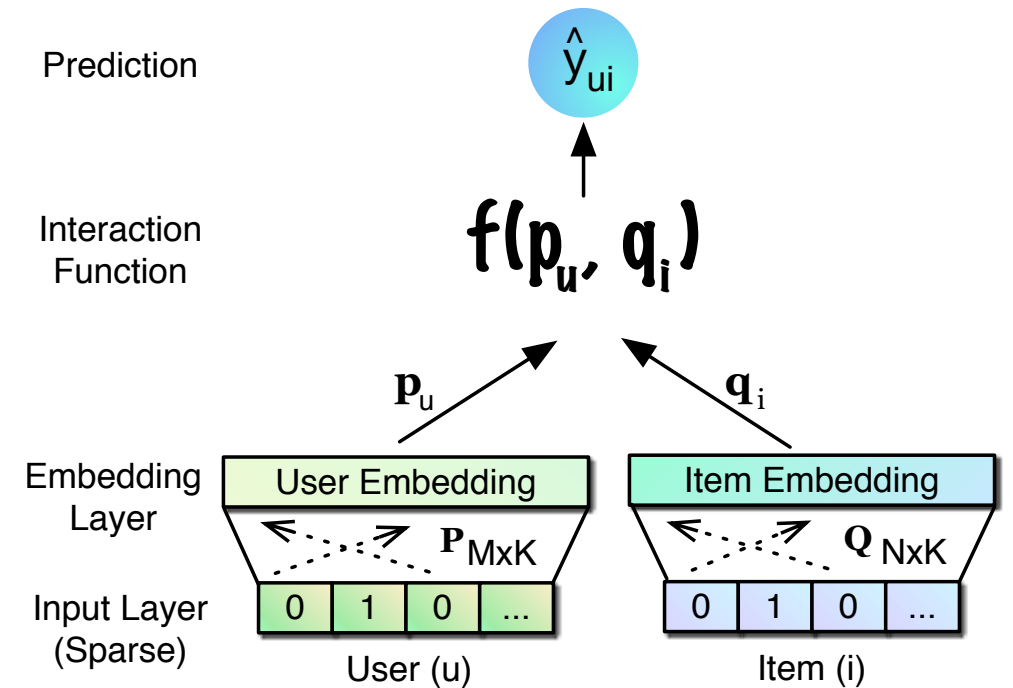
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- A prevalent model for collaborative filtering
 - Represent a user (or an item) as a vector of latent factors (also termed as *embedding*)



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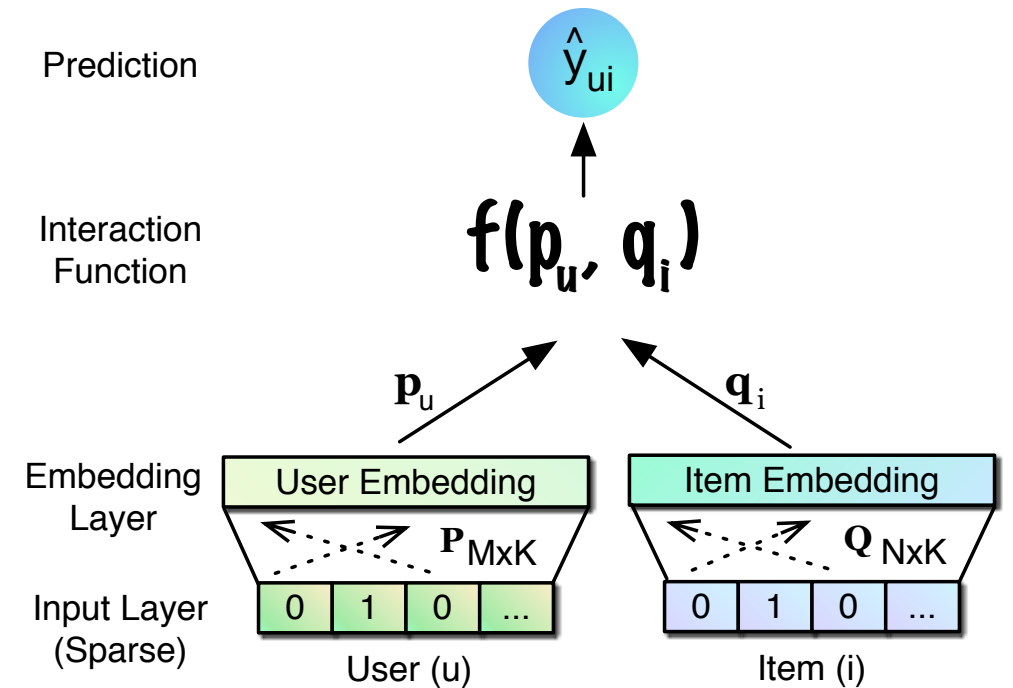


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➤ Many extensions on MF

- Model perspective: NeuMF [He et al, WWW'17], Factorization Machine etc.
- Learning perspective: BPR, Adversarial Personalized Ranking [He et al, SIGIR'18]



- MF uses **Inner Product** as the interaction function
- The **implicit assumption** in Inner Product:
 $f(\mathbf{p}_u, \mathbf{q}_i) = \mathbf{p}_u^T \mathbf{q}_i = \sum \begin{pmatrix} p_{u1} q_{i1}, \\ p_{u2} q_{i2}, \\ \dots \\ p_{uk} q_{ik} \end{pmatrix}$
 - The embedding dimensions are independent with each other

However, the implicit assumption is **impractical**.

- ❑ The embedding dimensions could be interpreted as certain properties of items [Zhang *et al.*, SIGIR'14], which are **not necessarily to be independent**

Recent DNN-based models either use **element-wise product** or **concatenation**.

- ❑ E.g., NeuMF [He *et al.*, WWW'17], NNCF [Bai *et al.*, CIKM'17], JRL [Zhang *et al.*, CIKM'17], Autoencoder-based CF Models [Wu *et al.*, WSDM'16]
- ❑ Still, the relations among embedding dimensions are **not explicitly modeled**.



Research Questions

- How to model the **relations** between embedding dimensions?
- Next:our proposed method:
 1. **Outer product** on user&item embedding for pairwise interaction modeling
 2. **CNN** on the outer product matrix to extract and reweight prediction signals.



Outer Product-based Neural Collaborative Filtering (ONCF)

Outer-product **explicitly** models the **pairwise relations** between embedding dimensions:

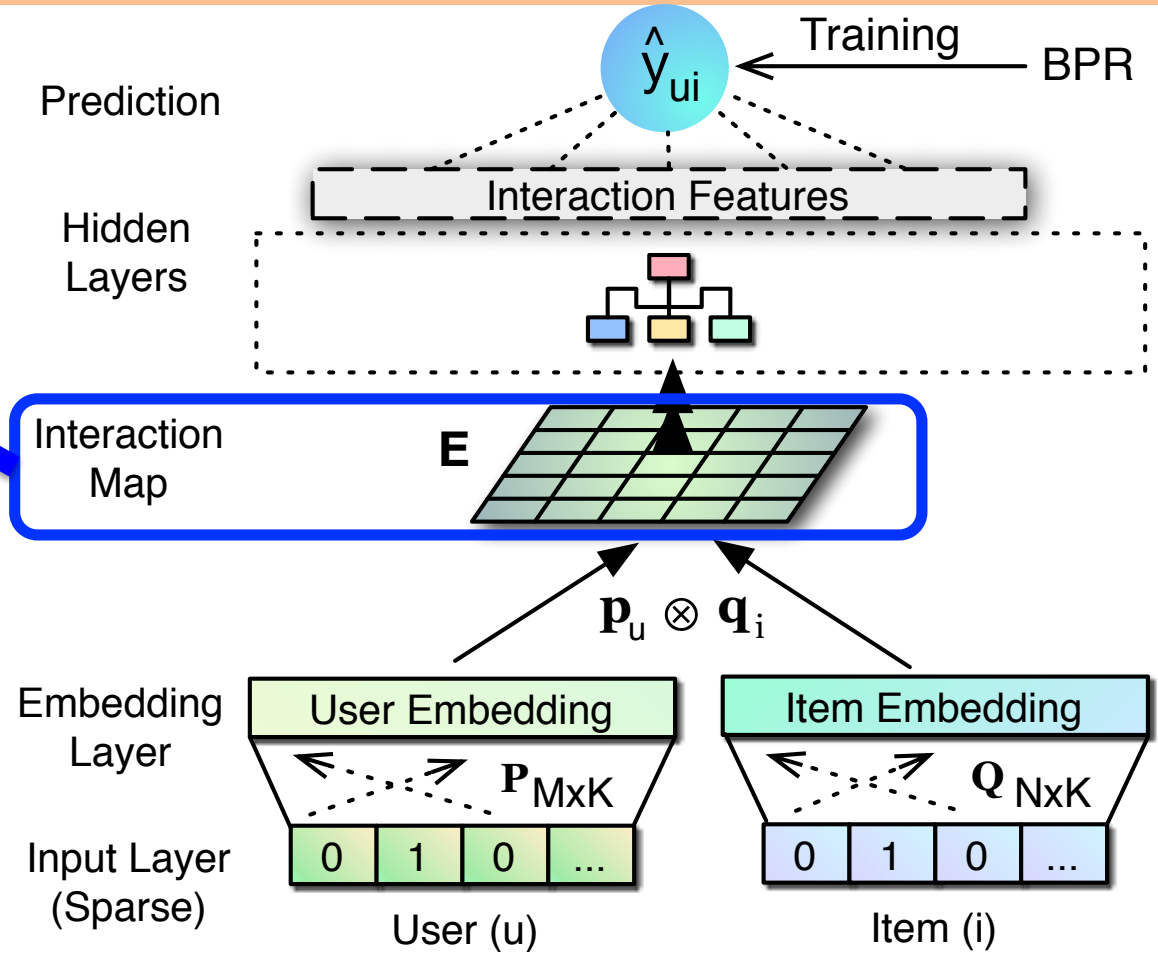
- Get a 2D matrix, named as **interaction map**:

Signals in Inner product

$$\mathbf{E} = \mathbf{p}_u \otimes \mathbf{q}_i = \mathbf{p}_u \mathbf{q}_i^T =$$

$$\begin{bmatrix} p_{u1}q_{i1} & p_{u1}q_{i2} & \dots & p_{u1}q_{ik} \\ p_{u2}q_{i1} & p_{u2}q_{i2} & \dots & p_{u2}q_{ik} \\ \vdots & \vdots & \ddots & \vdots \\ p_{uk}q_{i1} & p_{uk}q_{i2} & \dots & p_{uk}q_{ik} \end{bmatrix}$$

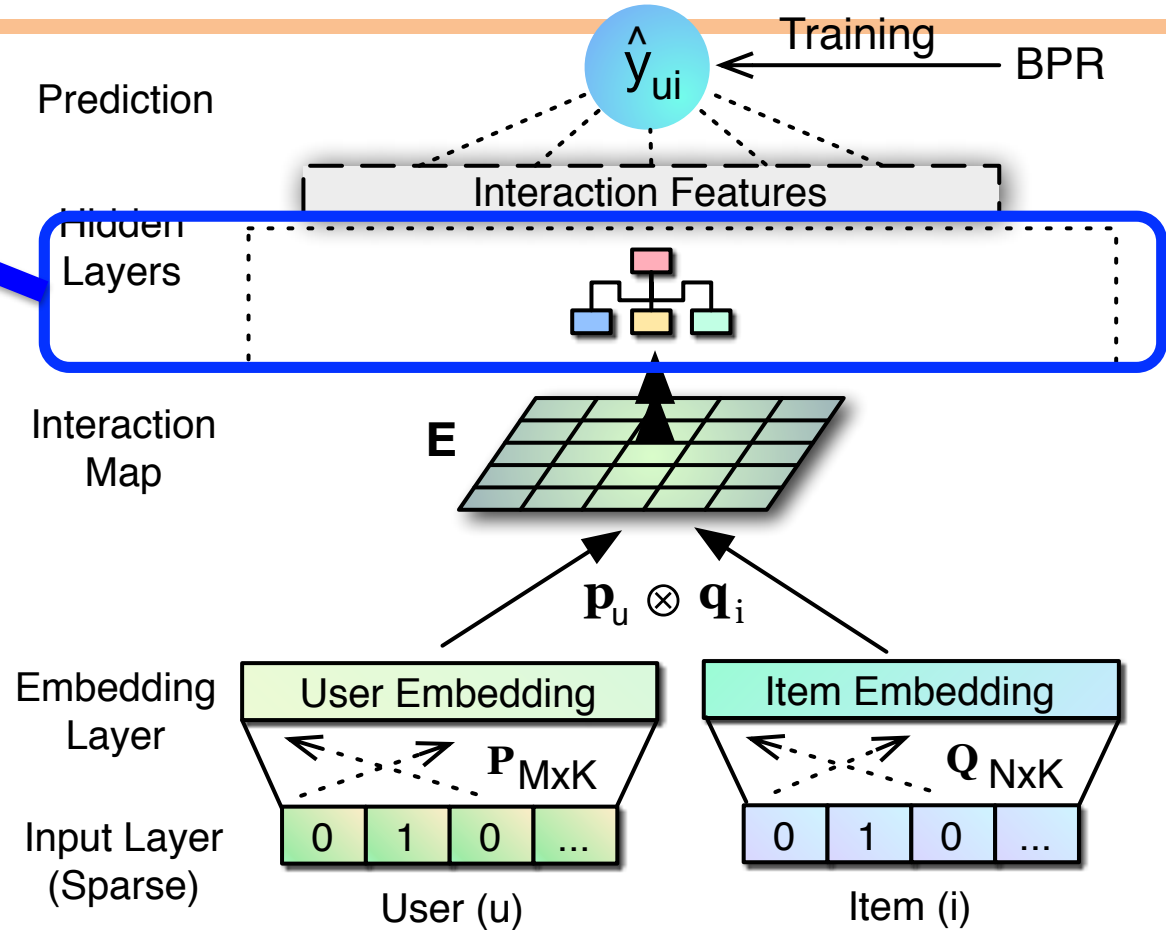
Indicating the interaction between the k-th dimension of \mathbf{p}_u and the 2-nd dimension of \mathbf{q}_i .



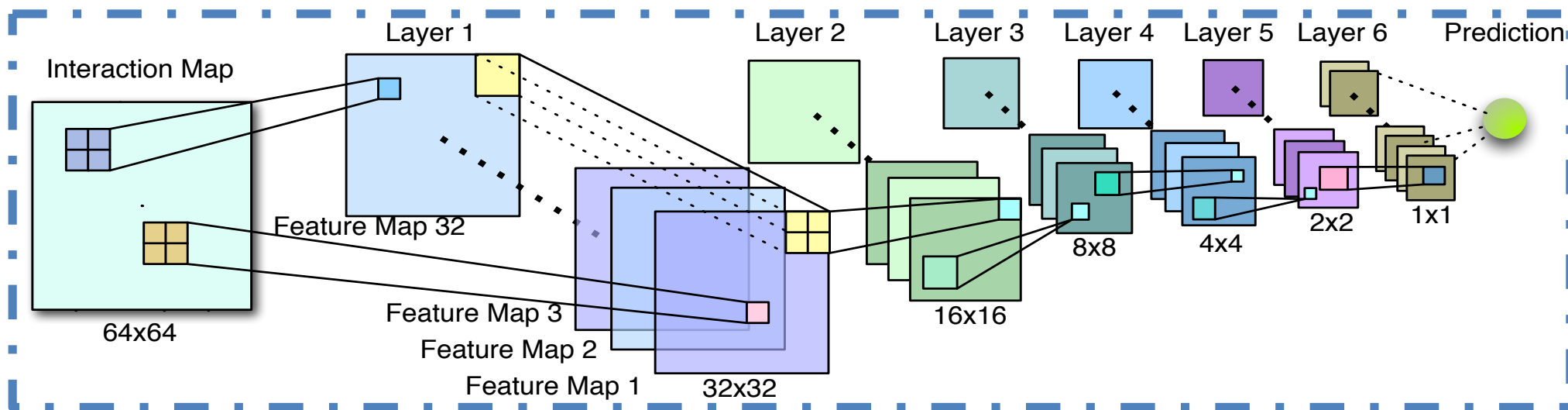
Above the interaction map are **hidden layers**, which aim to extract useful signal from the 2D interaction map.

A straightforward solution is to use MLP, however it results in too many parameters:

- Interaction map E has $K \times K$ neurons (K is embeddings size usually hundreds)
- Require **large memories** to store the model
- Require **large training data** to learn the model well



- ConvNCF uses locally connected CNN as hidden layers in ONCF:
 - CNN has **much fewer parameters** than MLP
 - Hierarchical tower structure: higher layer integrates more information from **larger area**.
 - Final prediction summarizes **all information** from interaction map.



- 2 Fully Connected Layers: **> 10M parameters**
- 6 Convolutional Layers: **20K parameters, but achieve better performance!**



Experimental Settings

➤ Datasets

- Yelp: 25,815 users, 25,677 items, and 730,791 interactions.
- Gowalla: 54,156 users, 52,400 items, and 1,249,703 interactions.

➤ Protocols

- Leave-one-out: holdout the latest interaction of each user as the test
- Pair 1 testing instance with 999 negative instances
- Top-K evaluation: ranking 1 positive vs. 999 negatives.
- Ranking lists are evaluated by Hit Ratio and NDCG (@10).

➤ Loss Function

- Bayesian Personalized Ranking



- MF-BPR [Rendle *et al.*, UAI'09]
 - Learning MF with a pair-wise classification loss.
- MLP [He *et al.*, WWW'17]
 - 3-layer multi-layer perceptron above user and item embeddings.
- JRL [Zhang *et al.*, CIKM'17]
 - Multi-layer perceptron above the element-wise product of embeddings.
- NeuMF [He *et al.*, WWW'17]
 - A neural network combining hidden layer of MF and MLP.

	Gowalla		Yelp		Average Improvement of ConvNCF over Baselines
	HR@10	NDCG@10	HR@10	NDCG@10	
MF-BPR	0.7480	0.5214	0.2817	0.1447	+9.5%
MLP	0.7590	0.5202	0.2831	0.1446	+9.1%
JRL	0.7747	0.5615	0.2922	0.1519	+4.3%
NeuMF	0.7793	0.5660	0.2958	0.1536	+3.3%
ConvNCF	0.7936*	0.5826*	0.3086*	0.1600*	-

* indicates that the improvements over all other methods are statistically significant for $p < 0.05$.

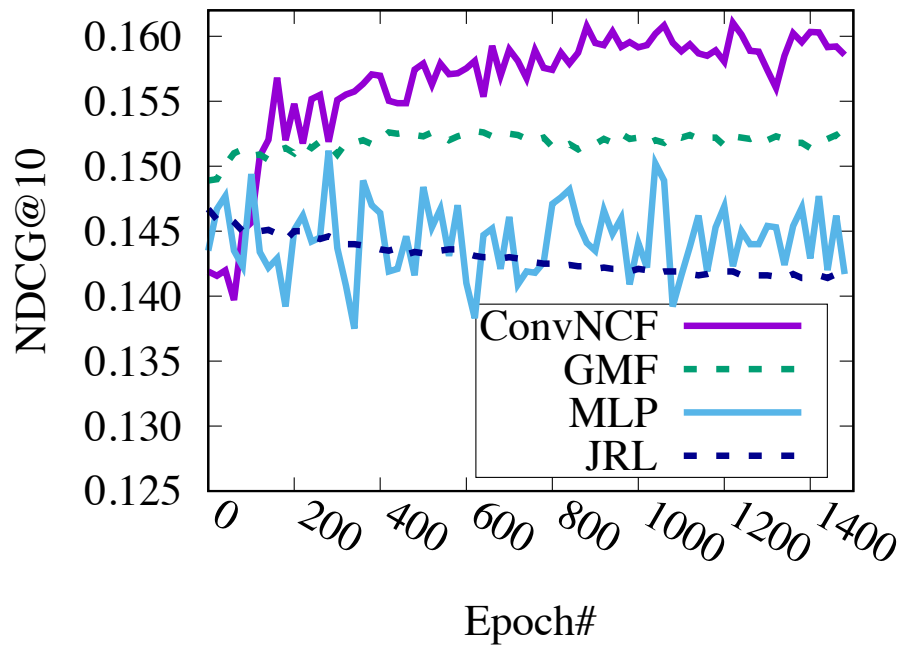
Overall Performance: ConvNCF > NeuMF[He et al., 2017] > **JRL**[Zhang et al., 2017]

- Usefulness of modeling the relations of embedding dimensions
- Training MLP well is practically difficult.

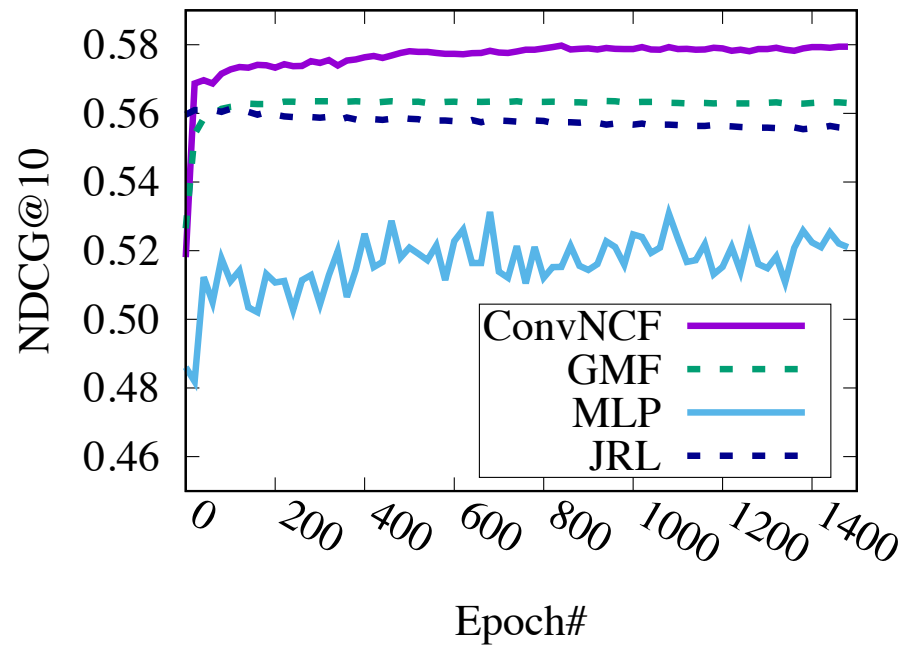
Training process of neural models that apply different operations above the embedding layer:

- ConvNCF: outer product; GMF: element-wise product; MLP: concatenation; JRL: element-wise product

Yelp



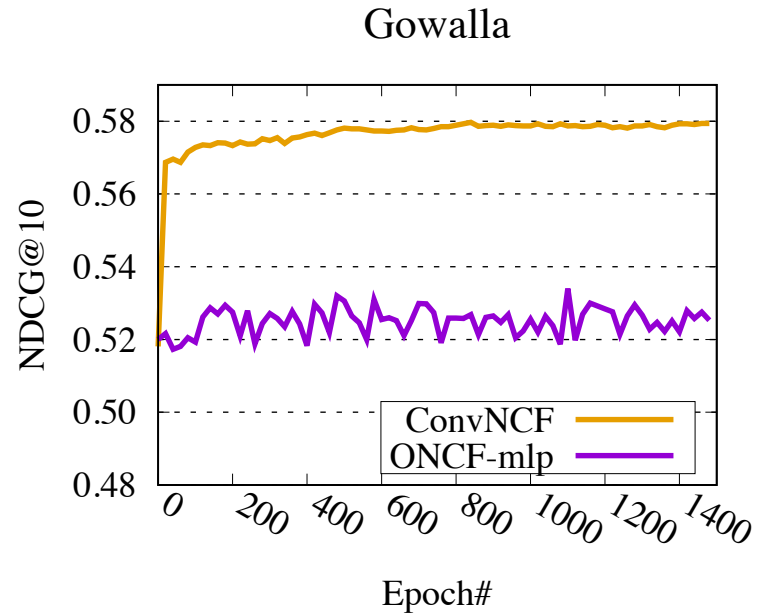
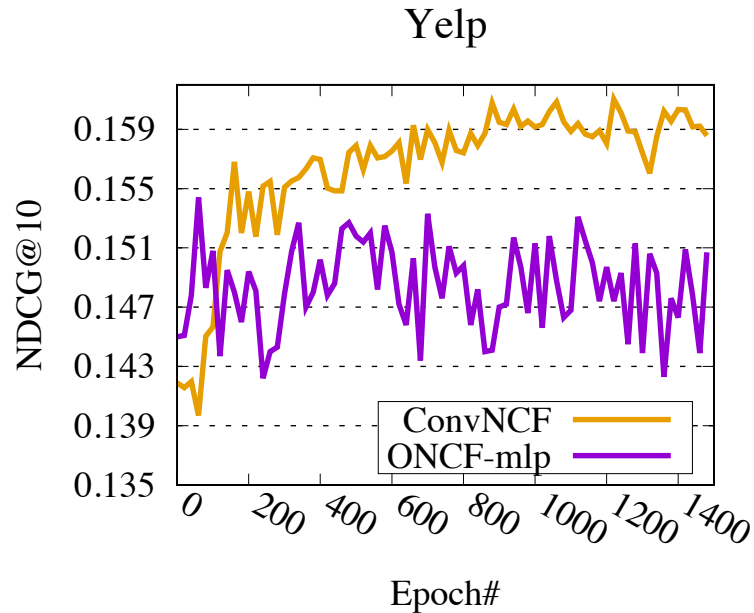
Gowalla



Outer product is a simple but effective merge of user&item embeddings.

NDCG@10 of using different hidden layers for ONCF:

- ConvNCF uses a 6-layer CNN.
- ONCF-mlp uses a 3-layer MLP above the interaction map.



1. ConvNCF outperforms ONCF-mlp.
2. ConvNCF is more stable than ONCF-mlp.



Conclusion & Future Work

Summary of contributions:

- A new neural framework for CF --- ONCF, which explicitly captures pairwise correlations between embedding dimensions with outer product
- A new model of ONCF framework --- ConvNCF, which uses CNN as hidden layers .
- Extensive experiments show effectiveness of ONCF framework and ConvNCF method.

Future work:

- We will explore more advanced CNN models to further explore the potentials of our ONCF framework.
- We will extend ONCF to content-based recommendation scenarios, e.g., items have image and textual content.



- [Xue *et al.*, 2017] Hong-Jian Xue, Xinyu Dai, Jianbing Zhang, Shujian Huang, and Jiajun Chen. Deep matrix factorization models for recommender systems. In *IJCAI*, pages 3203–3209, 2017.
- [Rendle *et al.*, 2009] Steffen Rendle, Christoph Freudenthaler, Zeno Gantner, and Lars Schmidt-Thieme. Bpr: Bayesian personalized ranking from implicit feedback. In *UAI*, pages 452–461, 2009.
- [He *et al.*, 2018] Xiangnan He, Zhankui He, Xiaoyu Du, and Tat-Seng Chua. Adversarial personalized ranking for item recommendation. In *SIGIR*, 2018.
- [Zhang *et al.*, 2014] Yongfeng Zhang, Guokun Lai, Min Zhang, Yi Zhang, Yiqun Liu, and Shaoping Ma. Explicit factor models for explainable recommendation based on phrase-level sentiment analysis. In *SIGIR*, pages 83–92, 2014.
- [Tay *et al.*, 2018] Yi Tay, Luu Anh Tuan, and Siu Cheung Hui. Latent relational metric learning via memory-based attention for collaborative ranking. In *WWW*, pages 729–739, 2018.
- [Bai *et al.*, 2017] Ting Bai, Ji-Rong Wen, Jun Zhang, and Wayne Xin Zhao. A neural collaborative filtering model with interaction-based neighborhood. In *CIKM*, pages 1979–1982, 2017.
- [He *et al.*, 2017] Xiangnan He, Lizi Liao, Hanwang Zhang, Liqiang Nie, Xia Hu, and Tat-Seng Chua. Neural collaborative filtering. In *WWW*, pages 173–182, 2017.
- [Zhang *et al.*, 2017] Yongfeng Zhang, Qingyao Ai, Xu Chen, and W Bruce Croft. Joint representation learning for top-n recommendation with heterogeneous information sources. In *CIKM*, pages 1449–1458, 2017.



THANK YOU!

Codes: <https://github.com/duxy-me/ConvNCF>

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